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STAFFMAN			

Applicant : Jonathan M. Friedman  
Application No. : 0,592 Filed: July 20, 2001  
For : A method for ab initio determination of macromolecular crystallographic phases at moderate resolution by symmetry enforced orthogonal multicenter spherical harmonic-spherical Bessel expansion.  
Attorney : James F. Haley, Jr., Reg. No. 27,794 Tel: (212) 596-9000

Docket No. : FAZIX/001 US  
Confirmation No. : 1403  
Sheet 1 of 7

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## Analysis of Packing Function Solutions for Monomeric Proteins

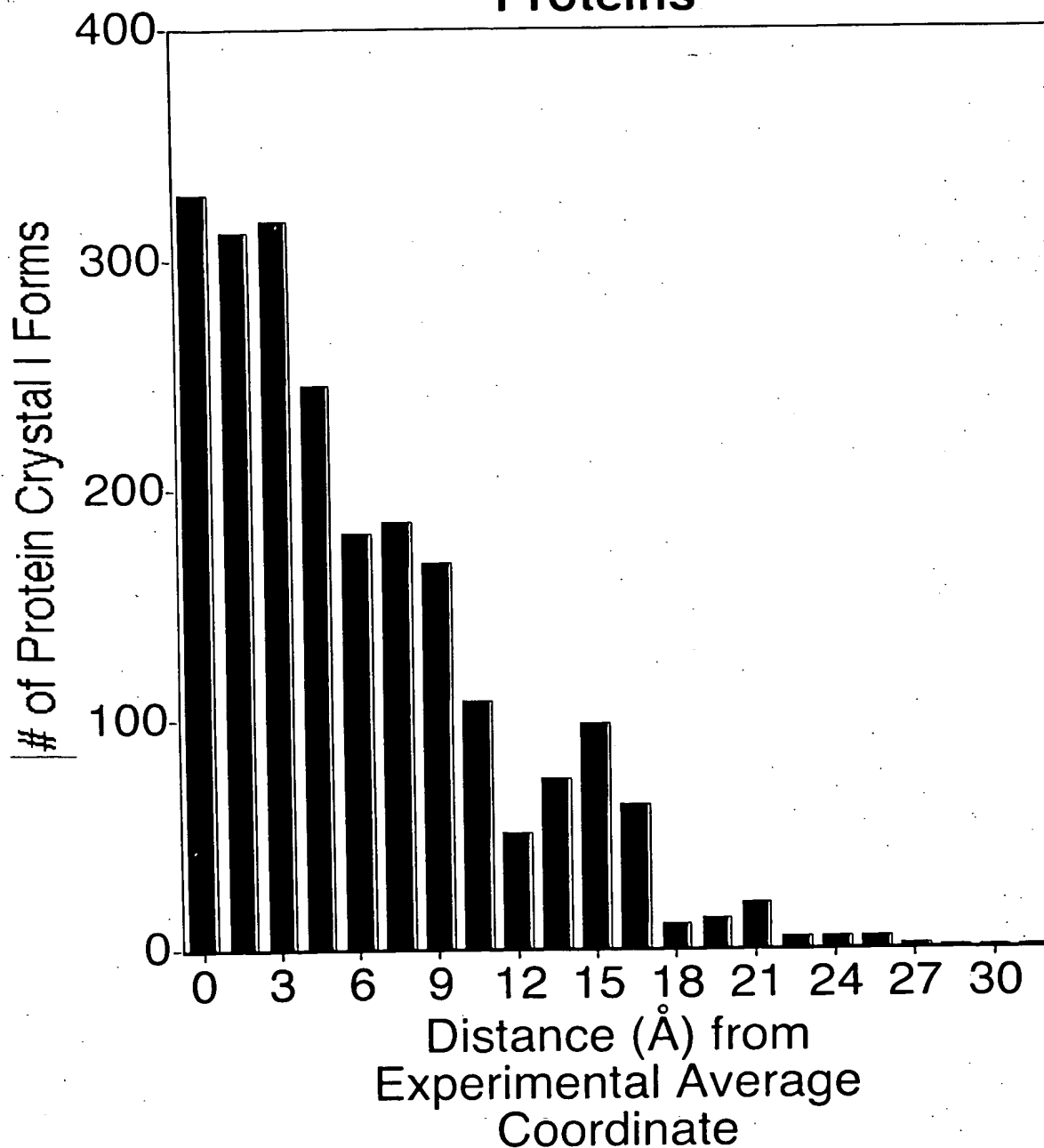


FIG. 1

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## Analysis of Packing Function Solutions for Monomeric Proteins

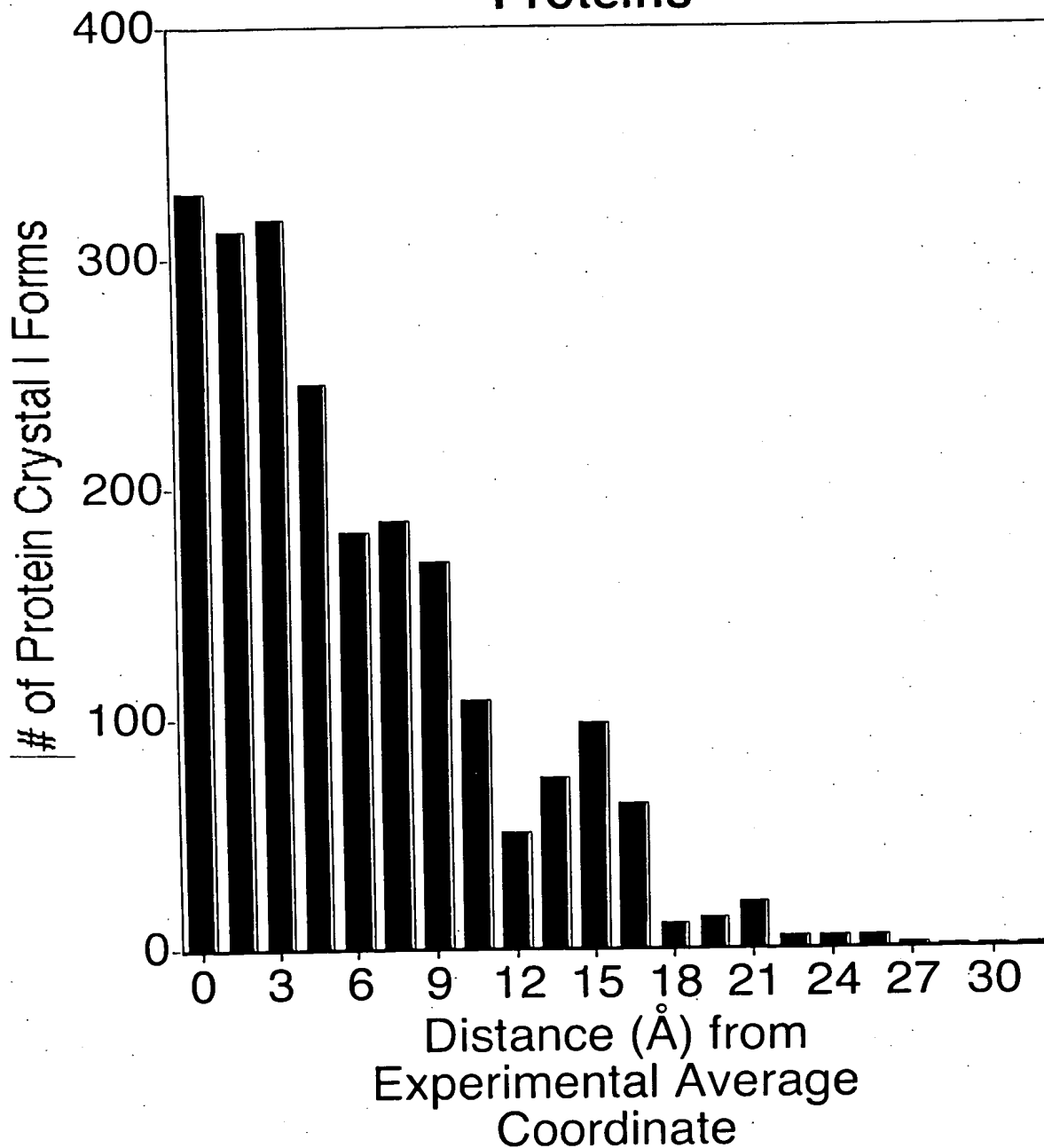


FIG. 2

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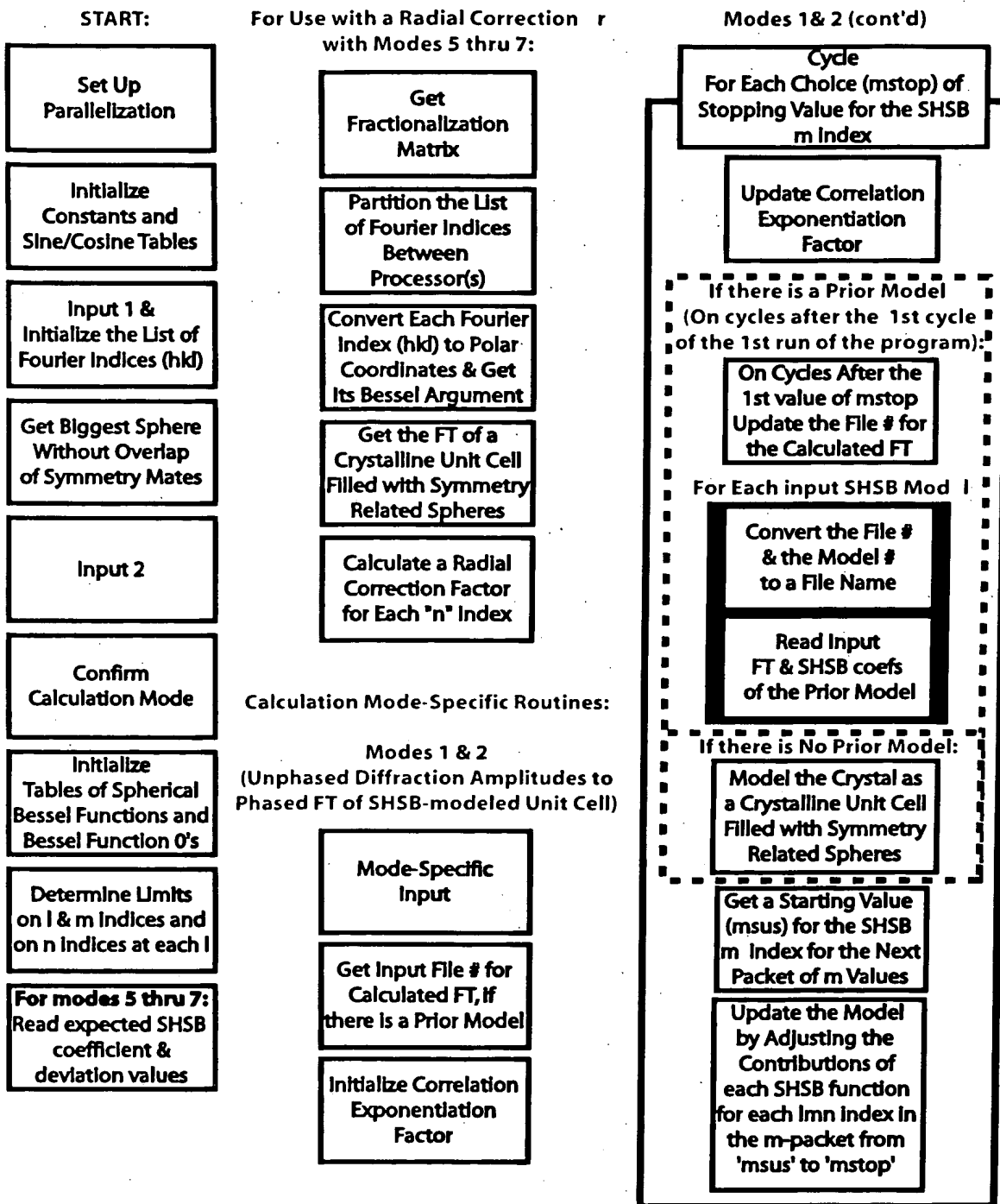


FIG. 3

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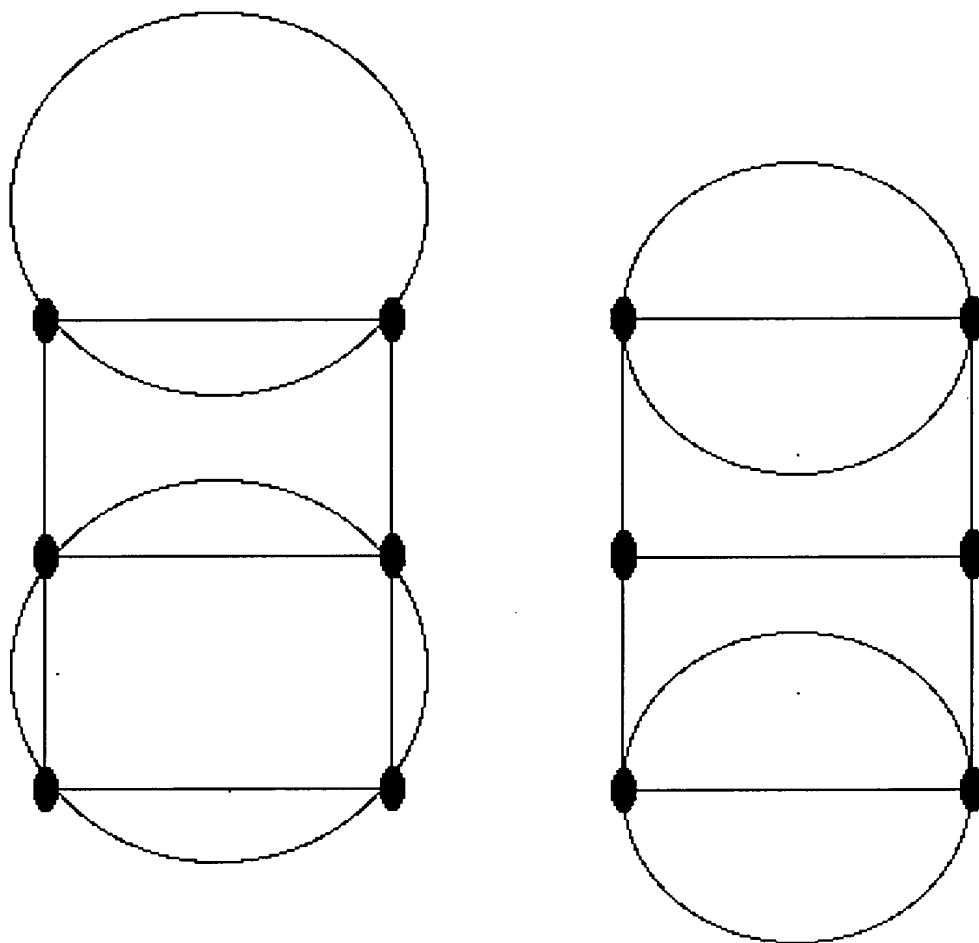
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**Figure .** A schematic example: Two choices for filling the same portion of a crystal unit cell from an orthorhombic Spacegroup. Although the spheres on the right are smaller than those on the left, for some crystals the local maximum in the packing on the right would be the packing of maximal consistency with the crystallographic data.

**FIG. 4**

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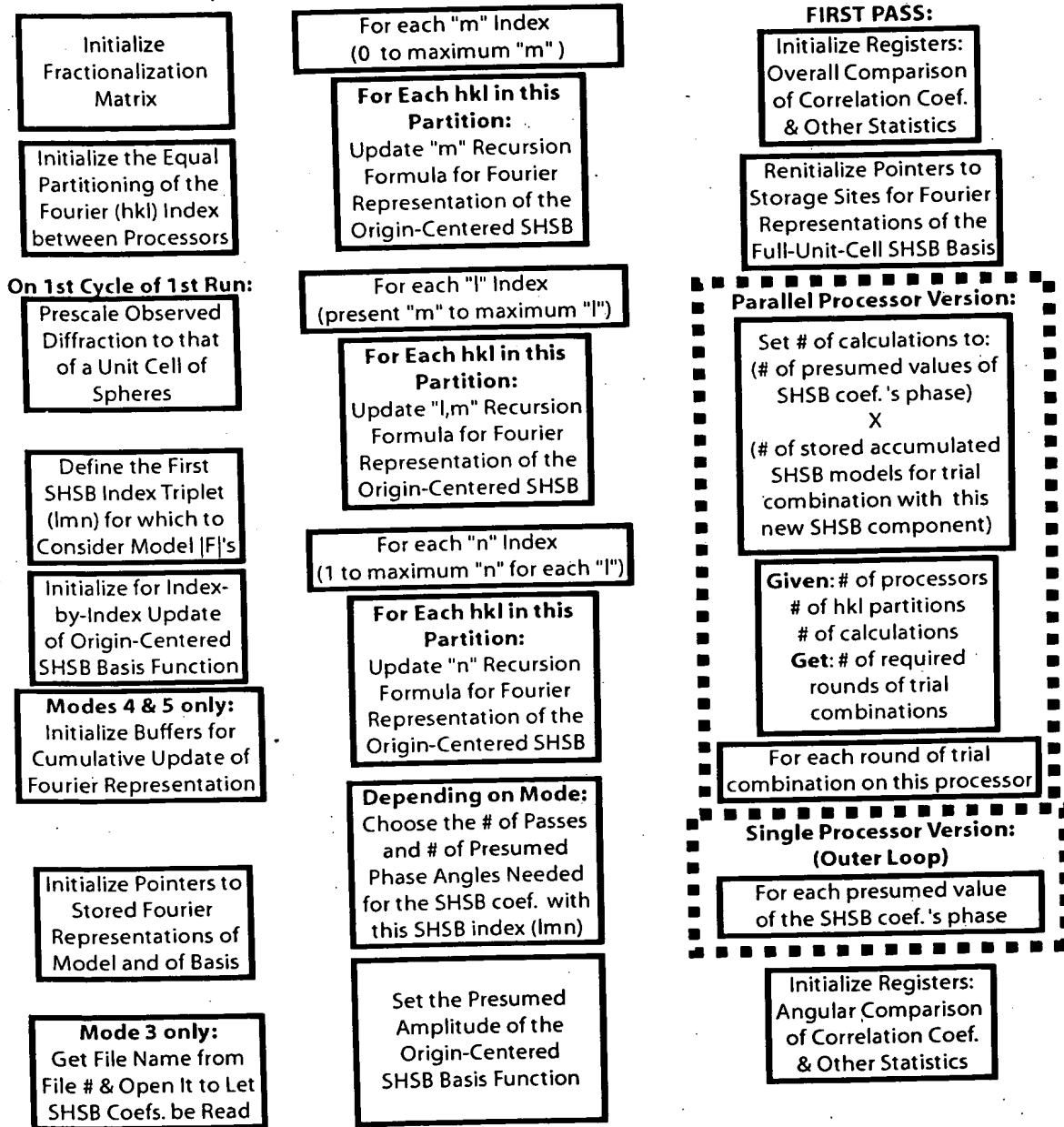


FIG. 5

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### Identical Image from Expansions about Different Origins:

$$\begin{aligned}
 & 11.22 x + 0.93e^{2\pi i(1.0) x} + 4.31e^{2\pi i(0.4) x} + \dots = \text{Image 1} \\
 & 10.01 x + 0.31e^{2\pi i(0.79) x} + 8.31e^{2\pi i(1.2) x} + \dots = \text{Image 2}
 \end{aligned}$$

Image 1 and Image 2 are identical, as indicated by the bracket connecting the two results.

### Symmetry Expanded Direct Space Basis Functions:

$$? x + ? e^{2\pi i(?) x} + ? e^{2\pi i(?) x} + \dots = \text{Expanded Image}$$

The diagram shows three rectangular boxes, each containing a different arrangement of spheres, representing basis functions. These are summed to produce a final box containing a complex, expanded image of the spheres.

With a properly chosen origin, 45-55% of the unit cell can be expanded. (Most protein crystals are > 45% solvent.)

FIG. 6

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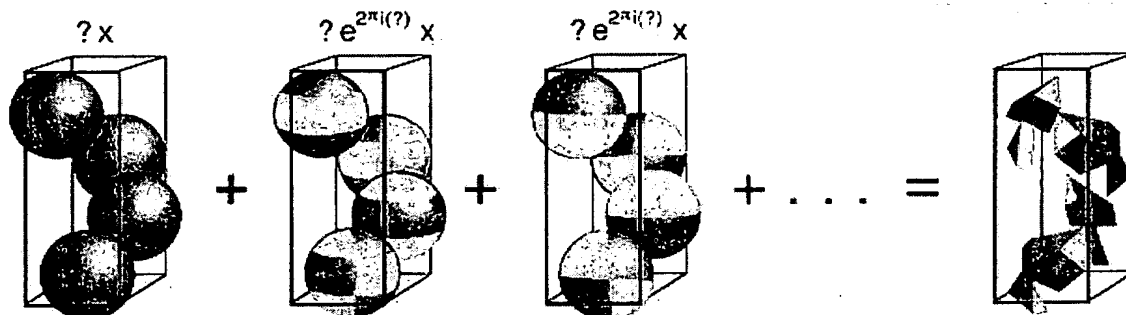
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### Component Direct Space Basis Functions:



### Component Fourier Transforms:

$$a_{001} F_{\text{solo}}^{001}(\text{hkl}) + a_{211} F_{\text{solo}}^{211}(\text{hkl}) + a_{111} F_{\text{solo}}^{111}(\text{hkl}) + \dots = F_{\text{obs}}(\text{hkl})$$

$$a_{001} = \sum_{\text{hkl}} F_{\text{solo}}^{*001}(\text{hkl}) F_{\text{obs}}(\text{hkl}) \quad [\text{presume } \phi = 0.00 \text{ to start}]$$

$$F_{\text{accum}}(\text{hkl}) = a_{001} F_{\text{solo}}^{001}(\text{hkl})$$

$$a_{211} = \sum_{\text{hkl}} F_{\text{solo}}^{*211}(\text{hkl}) (|F_{\text{obs}}(\text{hkl})| - |F_{\text{accum}}^n(\text{hkl})|) e^{2\pi i \phi_{\text{accum}}^n(\text{hkl})}$$

$$F_{\text{accum}}^{n+1}(\text{hkl}) = F_{\text{accum}}^n(\text{hkl}) + a_{211} F_{\text{solo}}^{211}(\text{hkl})$$

FIG. 7

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